

## Section 7.6 Confidence Intervals for a Population Mean ( $\mu$ ) ( $\sigma$ is unknown).

1. Gather  $\bar{x}$ ,  $s = \text{sample std. dev.}$ ,  $n$ , level of conf.  
Verify  $n > 30$  or pop. is normal.

2.  $\alpha = 1 - (\text{level of confidence})$

3. Look up  $t_{\alpha/2}$  on Table A2.

|       |                                       |
|-------|---------------------------------------|
| df    | <del><math>\alpha</math></del> 2-tail |
| ↓     | ↓                                     |
| $n-1$ | → $t_{\alpha/2}$                      |

4.  $E = t_{\alpha/2} \cdot \frac{s}{\sqrt{n}}$  ← max. error

5. Conf. interval:  $\bar{x} - E < \mu < \bar{x} + E$ .

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The mean hours of sleep for 35 (random) Mt. SAC students was 3.4 hours a night, with a std. dev of 1.6 hours. Construct a 96% Confidence interval for the mean hours of sleep of all Mt SAC students.

1.  $\bar{x} = 3.4$ ,  $s = 1.6$ ,  $n = 35 > 30 \checkmark$ , Conf = 0.96

2.  $\alpha = 1 - \text{conf} = 1 - 0.96 = 0.04$

3. Table A2

|    |                |
|----|----------------|
| df | $\alpha = .04$ |
| ↓  | 2-tail         |

|        |         |
|--------|---------|
| $n-1$  | ↓       |
| $= 34$ | → 2.136 |

4.  $E = t_{\alpha/2} \cdot \frac{s}{\sqrt{n}} = 2.136 \cdot \frac{1.6}{\sqrt{35}} \approx 0.58$

5.  $\bar{x} - E < \mu < \bar{x} + E$

$3.4 - 0.58 < \mu < 3.4 + 0.58$   
 $2.82 < \mu < 3.98$ .