

Section 5.1 → Discrete Random Variables

Discrete Random Variable X → quantity
 → assumes all possible results of an observation
 → gaps exist between consecutive values

Discrete Probability Distribution
 → associates a probability to each possible value of x .

John Kerrich's Coin

$$P(\text{heads}) \approx 0.51$$

Toss the coin 2 times, let X be the number of heads.

x	$P(x)$	$xP(x)$	$x^2P(x)$
0	.2401	0	0
1	.4998	.4998	.4998
2	.2601	.5202	1.0404
	1.0000	1.0200	1.5402

$$\mu = \sum x \cdot P(x) = 1.02$$

$$\sigma = \sqrt{\sum x^2 P(x) - \mu^2}$$

$$= \sqrt{1.5402 - 1.02^2}$$

$$= .7070$$

$$\text{Variance} = \sigma^2 = .4998$$

$$P(0) = P(T \frac{1}{2} T) = P(T) \cdot P(T) = .49 \cdot .49 = .2401$$

$$\begin{aligned} P(1) &= P(T \frac{1}{2} H \text{ or } H \frac{1}{2} T) = P(T \frac{1}{2} H) + P(H \frac{1}{2} T) \\ &= P(T) \cdot P(H) + P(H) \cdot P(T) \\ &= .49 \cdot .51 + .51 \cdot .49 \\ &= .4998 \end{aligned}$$

$$P(2) = P(H \frac{1}{2} H) = P(H) \cdot P(H) = .51 \cdot .51 = .2601$$

